The Density Functional Tight Binding (DFTB) Approach for Investigating Vacancy and Doping in Graphene as Hydrogen Storage

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Abstract
A study on graphene defects for hydrogen storage has been successfully conducted using the Density Functional Tight Binding (DFTB) approach. The research aimed to modify solid materials for hydrogen storage. A 4 × 4 × 1 unit cell was used as the basis, while the supercell used for sampling was enlarged to 40 × 40 × 1. The analyzed data included changes in Density of States (DOS), Fermi level shifts, electronic band structures, formation energy, adsorption energy, and isosurfaces for each graphene orientation. It has been observed that modifying the surface structure of graphene can alter the electronic properties of graphene. This is indicated by shifts in DOS intensity, characterized by increased electronic intensity around the Fermi level total density charge different. The interaction energy between graphene and hydrogen gas has been determined to be -0.0155 eV for H-epoxy graphene, -0.4941 eV for H-monovacancy graphene, and -0.0424 eV for HN-monovacancy graphene. The presence of the vacancy increase the potential to adsorp hydrogen.

Keywords: DFTB, graphene, graphene defects, hydrogen gas, hydrogen storage.

Introduction
Currently, there are several methods of hydrogen storage, including compressed gas, liquefaction, and adsorption, each with its own advantages and disadvantages. Solid-state hydrogen storage has the potential for high energy density and low weight, but so far, no commercial solution has been found. Therefore, the biggest challenge lies in discovering an effective way to store and transport hydrogen. 

CNT and graphene nanoflakes theoretically possess high hydrogen storage capacities [3]-[6]. The presence of alkali metals on the graphene surface can enhance hydrogen storage capabilities by creating additional surface sites for hydrogen adsorption [7][8]. Researchers have employed a combination of high temperature and chemical vapor deposition to create graphene with controlled vacancy density, resulting in an increased hydrogen storage capacity compared to pure graphene [9][10].

Modified graphene exhibits distinct properties compared to pure graphene. The active regions of modified graphene can shift the Fermi level above the Dirac point and alter the Density of States (DOS) near the Fermi level, leading to the formation of a bandgap between the conduction and valence bands [11]-[14]. This bandgap phenomenon is critical as it influences
the interaction between graphene and adsorbed molecules. In general, materials with wider bandgaps tend to have weaker adsorption interactions with other molecules, while those with narrower bandgaps tend to exhibit stronger adsorption interactions \cite{15,16}. When hydrogen is excessively adsorbed onto graphene, it becomes challenging to release as an energy source, and when adsorption is too weak, its capacity as a hydrogen carrier diminishes. The magnitude of the bandgap in graphene can be finely tuned through modifications involving vacancies, doping, and the introduction of alkali metals such as potassium.

The relationship between the influence of graphene structure, its electronic properties, and the strength of hydrogen gas adsorption needs to be comprehended at the molecular level. Quantum calculation methods are at the forefront in addressing this issue. However, to compute large-scale systems involving thousands of atoms, faster methods are required without compromising accuracy. In a periodic system, a layer of graphene comprises large carbon atoms, making it challenging for DFT and ab initio methods to handle calculations involving hundreds of atoms. Here, we showcase the validity, speed, and reliability of the DFTB method in modeling supercell graphene while evaluating their electronic properties during hydrogen adsorption. Concurrently, we're investigating modified graphene featuring vacancies, epoxy groups, and nitrogen-doped vacancy graphene to refine these characteristics and assess its capacity for attracting hydrogen.

**Experimental**

**Methods**

The crystal structure of graphene refers to Kristin Persson's work\cite{17}. The unit cell structure of graphene is constructed from the crystal unit cell of graphite with the following parameters: lattice parameters $a$, $b$, and $c$ are 2.468 Å, 2.468 Å, and 8.685 Å, respectively. The lattice angles $\alpha$, $\beta$, and $\gamma$ are 90°, 90°, and 120°, respectively. The lattice coordinates for the four carbon atoms are as follows: 0, 0, $\frac{3}{4}$; 0, 0, $\frac{1}{4}$; $\frac{1}{2}$, $\frac{1}{2}$, $\frac{3}{4}$; and $\frac{3}{2}$, $\frac{1}{2}$, $\frac{1}{4}$. The crystal system adheres to a hexagonal structure with a point group of $6/mmm$.

To produce graphene layers, the original graphite unit cell is enlarged to a 4 $\times$ 4 $\times$ 1 unit cell using the VESTA software \cite{18}. The procedure for creating vacancy and N-doped modified graphene follows the approach outlined by Hidayat et al., \cite{19,20}. The addition of oxygen atoms on top of two carbon atoms in the center of the cell transforms pristine graphene into an epoxy graphene model. In the geometry optimization calculations, the unit cell was expanded into a supercell with dimensions of 40 x 40 x 1. The optimization calculations were conducted with the application of Periodic Boundary Conditions (PBC) using the Self-Consistent Charges-Density Functional Tight Binding (SCC-DFTB) method.

The Slater-Koster mio parameters were employed as DFTB parameters for interatomic interactions. The Fermi smearing method at a temperature near 0 K was employed to generate conserved orbital functions. The k-points in the Brillouin zone were set at $\Gamma$ (0,0,0), M (0,0,0), and K (0,0,0). Subsequently, the supercell was optimized until convergence was achieved. The calculation was performed by the DFTB+ software\cite{21}.

Modeling the adsorption of hydrogen gas is carried out by positioning hydrogen molecules above the centers of all optimized graphene sheets. The hydrogen molecules are vertically oriented, directing the hydrogen atoms towards the vacancy and doping sites of the graphene. The optimization procedure was then repeated.

The optimized-state calculations provided data on the density of states (DOS), Fermi level, atomic charges, and band energy structure for each model. The calculation of these electronic parameters depends on the geometry of the modeled system. The modeled system is
considered ideal when it possesses the lowest energy and its values align with a valid reference. Subsequently, the DOS graph and band structure were adjusted to align with a Fermi level of 0 eV, as determined by $E_0-E_F$. $E_0$ represents the reference Fermi level set at 0 eV, while $E_F$ denotes the calculated Fermi level.

The formation energy of the GO surface containing either "n" epoxy groups denoted as $E_f$ is calculated using equation 1 [20]

$$E_f = E_{GO} - E_{PG} - nE_O$$  \hspace{1cm} (1)

Where $E_{GO}$, $E_{PG}$, and $nE_O$ represent the total energy of the graphene with epoxy group, pure graphene, and the number of free epoxy groups (O atoms), respectively. The energy $E_O$ is obtained by optimizing $O_2$ using the same optimization procedure, with the resulting energy divided by two.

The formation energy of nitrogen-modified monovacancy graphene can be calculated using the equation 2

$$E_f = E_{tot} - n_NE_N + n_CE_C - E_{PG}$$  \hspace{1cm} (2)

Here, $E_{tot}$ represents the total energy of the modified graphene with vacancies or doping.

The variables $nN$ and $E_N$ correspond to the number of atoms and the energy of the N-dopant, while $nC$ and $E_C$ refer to the number of removed carbon atoms and its energy. Lastly, the $E_{PG}$ represents the total energy of pristine, unmodified graphene.

The interaction energy of hydrogen adsorption on the graphene surface, in terms of adsorption energy ($E_{ads}$), is calculated using the equation 3

$$E_{ads} = E_{complex} - (E_{GM} + E_{hydrogen})$$  \hspace{1cm} (3)

In this equation, $E_{complex}$ represents the energy of the hydrogen model adsorbed on the modified graphene surface, $E_{GM}$ is the energy of the modified graphene, and $E_{hydrogen}$ is the energy of the H$_2$.

Results and Discussion

The optimization of graphene's structure was performed using the DFTB (Density Functional Tight Binding) method within its crystal lattice vectors x, y, and z. In the accompanying image, carbon atoms are depicted in brown, oxygen atoms in red, nitrogen atoms in silver, and hydrogen atoms in white. The optimization results for graphene are visualized in the Figure 1.

Figure 1. Visualization of optimized graphenes without and with adsorbed hydrogen (a) Vacancy graphene (b) N-doped vacancy graphene and (c) Epoxy functionalized graphene. Brown, cyan, red and with refer to C, N, O and H, respectively.
The geometry optimization for monovacancy graphene reveals C-C bond distances ranging from 1.4142 to 1.4603 Å. However, based on XRD, EXAFS, and EDX analyses, pristine graphene exhibits highly symmetrical single distances at 1.42 Å [22]-[24]. This confirms that the symmetry is reduced around the vacancy site. The presence of Hydrogen change influences the C-C distance of the graphene ranging from 1.4045 to 1.4596 Å, and the H₂ molecule closed to one of the carbon atoms (C-H) in the vacancy site at a distance of 2.3816 Å.

In monovacancy N-graphene, the carbon-carbon (C-C) bond distance falls within the range of 1.4137 to 1.5128 Å, while the nitrogen-carbon (N-C) bond distance is approximately 1.3413 Å. These findings closely concistence with data obtained through Density Functional Theory (DFT) calculations, which typically predict C-C bond distances in the range of approximately 1.41 to 1.45 Å [25],[26]. On the other hand, in the presence of H₂, the C-C bond distance ranges from 1.4139 to 1.5127 Å, and the C-N bond distance is around 1.3411 Å. These results suggest that there is no significant effect on the graphene structure when hydrogen (H₂) is adsorbed.

The optimization results for epoxy graphene show that the distance between carbon atoms (C-C) ranges from 1.4140 to 1.5135 Å, while the distance between carbon and oxygen atoms (C-O) ranges from 1.4964 to 1.4965 Å. For hydrogen-functionalized graphene epoxy, the C-C distance ranges from 1.4139 to 1.5129 Å, and the C-O distance ranges from 1.4979 to 1.4980 Å. The presence of hydrogen on the surface did not significantly influence the structure of graphene. The distance was found to be equal using both the ab initio and DFT methods [27][30]. Additionally, the distance between H₂ atoms is 0.7451 Å, and the closest distance between an H atom and an O atom is 2.235 Å.

Based on the calculations, it was found that epoxy graphene has a formation energy of -3.3721 eV. These results align with the research conducted by Prasert and Sutthubutpong using the DFT method, which reported a formation energy for epoxy graphene ranging from -3.092 eV to -3.231 eV [30]. Meanwhile, for monovacancies, the DFTB method yielded a formation energy of 8.2594 eV, which is in close agreement with previous research by Ali and colleagues, who used the DFT method and reported values between 7.19 and 7.78 eV [31]. In the case of N-graphene monovacancies, the obtained formation energy is 5.9785 eV. Positive formation energy values indicate thermodynamic instability. The formation energy values for all three types of graphene are consistent with the DFT calculation method. Table 1 show in details the formation energi with other methods.

Figure 2 shows all comparison of DOS graphene before and after adsorb hydrogen. The fermi level has been shift to the refence point (0). Based on the graph, it is evident that the interaction between epoxy graphene and hydrogen gas does not significantly alter the DOS spectra. There is only a minor increase in electronic intensity within the valence band region at approximately -4 eV to -3 eV (Figure 2a).

<table>
<thead>
<tr>
<th>Struktur</th>
<th>Metode</th>
<th>Ef (eV)</th>
<th>Fermi Level (eV)</th>
<th>Ref</th>
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<td>-4.5</td>
<td>[32]</td>
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</table>

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The interaction between hydrogen gas and monovacancy graphene indeed alters the Density of States (DOS) spectra precisely at the Dirac point in the Fermi level region. This is because hydrogen adsorbs at the vacancy site, leading to an increase in intensity at that specific point (Figure 2b). The interaction between hydrogen gas and N-graphene monovacancy does not significantly alter the Density of States (DOS) spectra. There is a minor increase in electronic intensity primarily within its conduction band region at approximately -4.5 eV to -3 eV, with only minimal changes observed in the rest of the conduction band (figure 2c).

Table 2. Interaction energy modeled graphenes with H₂

<table>
<thead>
<tr>
<th>Graphene</th>
<th>Method</th>
<th>$E_{ads}$ (eV)</th>
<th>Reference</th>
</tr>
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<td>This work</td>
</tr>
<tr>
<td>Monovacancy graphene</td>
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<td>-0.4941</td>
<td>This work</td>
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<tr>
<td></td>
<td>DFT</td>
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<td>[9]</td>
</tr>
<tr>
<td>N-monovacancy graphene</td>
<td>DFTB</td>
<td>-0.0424</td>
<td>This work</td>
</tr>
<tr>
<td></td>
<td>DFT</td>
<td>-0.04</td>
<td>[10]</td>
</tr>
<tr>
<td></td>
<td>DFT</td>
<td>-0.059</td>
<td>[11]</td>
</tr>
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</table>

Figure 2. DOS comparison before and after adsorb Hydrogen (a) Epoxy graphene (EG) (b) Monovacancy graphene (VG) (c) N-monovacancy graphene (NVG)
Table 2 displays the hydrogen adsorption energies on graphene. Based on the calculations, the interaction energy for H-epoxy graphene is -0.0155 eV, for H-monovacancy graphene it is -0.0424 eV, and for H-N-monovacancy graphene it is -0.4941 eV. The DFT method yielded hydrogen adsorption energies on monovacancy graphene ranging from -0.3282 eV to -0.402 eV [9]. This indicates that the DFTB method demonstrates good validity for modeling H$_2$ gas adsorption on various graphene models. Additionally, graphene monovacancy doped with N shows adsorption capabilities equivalent to potassium-doped graphene (-0.04 eV)[10]. Other research reports that N-doped graphene can adsorb hydrogen with an energy of -0.059 eV[11]. Here the adsorption hydrogen tend to follow physisorption mechanism.

The potential energy interaction scan of H$_2$ with graphene was conducted to observe the equilibrium bond distance between H$_2$ and graphene. It’s important to note that the distance of H$_2$ on graphene with vacancies is calculated from the midpoint of the vacancy surface, and this distance varies vertically. With the exception of epoxy graphene, the varied H$_2$ distance is measured from the epoxy. The potential energy scan between H$_2$ and modeled graphene, as a function of distance, is depicted in Figure 3. Sequentially, the closest distances between hydrogen and the graphene surface are as follows: in monovacancy graphene (2.0 Å), nitrogen-doped monovacancy graphene (2.0 Å), and epoxy graphene (2.2 Å). This sequence arises as a consequence of their adsorption energies. Geometry optimization within the equilibrium distance range resulted in the following interaction distances of H$_2$ with the nearest atoms: H$_2$-O on epoxy graphene at 2.23 Å, H$_2$-N on nitrogen-doped monovacancy graphene at 2.06 Å, and the closest H$_2$-C on monovacancy graphene at 2.381 Å.

The orientation of hydrogen adsorption on the graphene surface is confirmed by the total charge difference between the graphene surface and hydrogen. Figure 3 shows that hydrogen is adsorbed vertically, with the hydrogen atoms having partial positive charges being directed towards the graphene surface, which has partial negative charges. The highest adsorption energy on graphene monovacancy is due to the presence of two carbon atoms in the vacancy site region with partial negative charges (Figure 3b).

![Figure 3. Potential Energy of adsorbed H2 on the modeled graphenes](image-url)
The interaction with N-monovacancy graphene is relatively stronger compared to epoxy, as evident from the larger size of the hydrogen charge density (shown in blue) in Figure 3c and Figure 3a. In general, the presence of vacancies enhances the interaction potential with hydrogen, while epoxy graphene allows hydrogen to move more freely, resulting in lower adsorption energy.

**Conclusions**

Adsorption of hydrogen on modeled graphene is mainly described as physisorption. The existence of hydrogen gas does not have a significant impact on graphene’s electronic properties. This makes sense since weak interactions do not possess the ability to strongly transfer charges. On the other hand, the presence of vacancies can increase the interaction potential between hydrogen and graphene. The DFTB approach has been successfully employed to explore and elucidate the relationship between the properties of modified graphene in adsorbing H₂.

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**References**


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